

**QUIZ 7: ABSTRACT ALGEBRA**

- A **permutation** of a set is a rearrangement of its elements.
- **Cycle notation** expresses permutations by denoting the elements cyclically moved by the permutation.
- The **order** of a permutation is the number of times the permutation must be applied to return to the original arrangement.

**Problem 1:** List all elements of  $S_3$  in cycle notation and determine their order.

**Problem 2:** Let  $\sigma = (123)$  and  $\tau = (12)$ . Compute  $\tau^{-1}$  and  $\tau\sigma\tau^{-1}$ . Write your answer in cycle notation

**Problem 3:** Consider the element of  $S_9$  below. Write the permutation below as a composition of cycles.

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \\ 4 & 3 & 2 & 7 & 6 & 5 & 9 & 1 & 8 \end{pmatrix}$$